A Kinetic Model of Single and Clustered IP₃ Receptors in the Absence of Ca²⁺ Feedback

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ABSTRACT Ca²⁺ liberation through inositol 1,4,5-trisphosphate receptor (IP₃R) channels generates complex patterns of spatiotemporal cellular Ca²⁺ signals owing to the biphasic modulation of channel gating by Ca²⁺ itself. These processes have been extensively studied in Xenopus oocytes, where imaging studies have revealed local Ca²⁺ signals ("puffs") arising from clusters of IP₃Rs, and patch-clamp studies on isolated oocyte nuclei have yielded extensive data on IP₃R gating kinetics. To bridge these two levels of experimental data, we developed an IP₃R model and applied stochastic simulation and transition matrix theory to predict the behavior of individual and clustered IP₃R channels. The channel model consists of four identical, independent subunits, each of which has an IP₃-binding site together with one activating and one inactivating Ca²⁺-binding site. The channel opens when at least three subunits undergo a conformational change to an "active" state after binding IP₃ and Ca²⁺. The model successfully reproduces patch-clamp data; including the dependence of open probability, mean open duration, and mean closed duration on [IP₃] and [Ca²⁺]. Notably, the biexponential distribution of open-time duration and the dependence of mean open time on [Ca²⁺] are explained by populations of openings involving either three or four active subunits. As a first step toward applying the single IP₃R model to describe cellular responses, we then simulated measurements of puff latency after step increases of [IP₃]. Assuming that stochastic opening of a single IP₃R at basal cytosolic [Ca²⁺] and any given [IP₃] has a high probability of rapidly triggering neighboring channels by calcium-induced calcium release to evoke a puff, optimal correspondence with experimental data of puff latencies after photorelease of IP₃ was obtained when the cluster contained a total of 40–70 IP₃Rs.

INTRODUCTION

The inositol 1,4,5-trisphosphate receptor (IP₃R) acts as a Ca²⁺ release channel to liberate Ca²⁺ ions from the endoplasmic reticulum (ER) into the cytosol (1). Structurally, the IP₃R is a large (~30 nm in diameter) homomeric tetramer of four subunits forming a single ion-conducting channel (2). Each subunit is composed of three functionally different domains, including a large cytoplasmic region of aminoterminal IP₃-binding domain, a carboxy-terminal channel-forming domain, and a middle coupling modulatory and transducing domain (3,4). Opening of the channel requires binding of the second-messenger inositol 1,4,5-trisphosphate (IP₃), which is generated in the cytoplasm in response to the binding of extracellular ligands to plasma membrane receptors. Moreover, gating of the IP₃R is biphasically modulated by Ca²⁺ ions, such that small elevations of cytosolic [Ca²⁺] promote channel opening, whereas higher [Ca²⁺] results in inactivation (5). This Ca²⁺ feedback underlies a process of Ca²⁺-induced Ca²⁺ release (CICR), resulting in regenerative liberation of Ca²⁺ that may either remain restricted to a cluster of IP₃Rs to generate a localized Ca²⁺ puff (6), or propagate as a saltatory wave across numerous puff sites by successive cycles of Ca²⁺ diffusion and CICR.

To elucidate the complex spatiotemporal patterns of Ca²⁺ signals generated by the IP₃ pathway, we need to understand the functioning of IP₃Rs at the single-molecule level, the spatial arrangement of these receptors in the cell, and their functional interactions via Ca²⁺ diffusion and CICR. The Xenopus oocyte provides a favorable cell system with which to investigate these topics, by virtue of the wealth of experimental data available regarding both the imaging of IP₃-evoked Ca²⁺ signals in the intact cell (6–8) and patch-clamp recordings of single IP₃Rs in the outer membrane of isolated oocyte nuclei (9–12). To bridge these two levels of experimental data, we developed an IP₃R model, and used both transition matrix theory and stochastic simulation to predict the behavior of individual and clustered channels.

Models of the IP₃R play a central role not only for the understanding channel kinetics, but also as building blocks for constructing larger-scale models of cellular Ca²⁺ signaling. Several IP₃R models (13–19) have been developed to describe experimental data obtained from IP₃R reconstituted in bilayer membranes, with broad application of the DeYoung-Keizer model (14) in particular. However, there are significant differences in behavior of the reconstituted IP₃Rs versus that of IP₃Rs in their native environment of the nuclear envelope, and only a few models have incorporated IP₃R data obtained on nucleus membranes. Among these, an allosteric four-plus-two-conformation model was considered by Mak et al. (11). That model postulates that each of the four IP₃R monomers has one IP₃-binding site and three...
different functional Ca\textsuperscript{2+}-binding sites on the cytoplasmic side of the channel. Another model was developed by Baran (20), consisting of one activation module and one inhibition module, both allosterically operated by Ca\textsuperscript{2+}, IP\textsubscript{3}, and ATP, together with one adaptation module, driven by IP\textsubscript{3} and Ca\textsuperscript{2+}. However, these two models can predict only the steady-state gating properties, and not the kinetics of individual channel openings and closings.

Thus, there has been no model that could realistically simulate the kinetic behavior of IP\textsubscript{3}R under physiological conditions in the Xenopus oocyte. Our aim was to develop a dynamic IP\textsubscript{3}R model that successfully reproduces data obtained from patch-clamp recordings of nuclear IP\textsubscript{3}Rs, and that is sufficiently simple and computationally tractable for application in future studies simulating the interactions of numerous IP\textsubscript{3}Rs coupled in a cellular environment by Ca\textsuperscript{2+} diffusion and CICR. The channel model consists of four identical, independent subunits, each of which has an IP\textsubscript{3}-binding site, together with one activating and one inactivating Ca\textsuperscript{2+} binding site. A feature of the model is that channel opening may occur if either three or four of the subunits of the tetramer are in an “activated” state (binding both IP\textsubscript{3} and the activating Ca\textsuperscript{2+} ion, but not the inhibitory Ca\textsuperscript{2+} ion), and we show how this characteristic can account for the observed biexponential distribution of open times and the dependence of mean open time on [Ca\textsuperscript{2+}]. Moreover, we extend our IP\textsubscript{3}R channel model to the cellular level by simulating the latency of puffs after step increases of IP\textsubscript{3}, on the assumption that the stochastic opening of a single IP\textsubscript{3}R within a cluster rapidly evokes CICR from neighboring channels with high probability to generate a puff. On this basis, we predict that puff sites contain a total of 40–70 IP\textsubscript{3}Rs.

**MODEL**

A schematic picture of the IP\textsubscript{3}R model is shown in Fig. 1, which, from structural studies (2), comprises four identical and independent subunits. Based on experimental observations that the channel open probability is a bell-shaped function of [Ca\textsuperscript{2+}] (5,10,15), we consider two independent Ca\textsuperscript{2+}-binding sites for each subunit; i.e., an activating binding site and an inhibitory site. Consistent with the molecular structure of the IP\textsubscript{3}R (3,4) and concordant with most previous IP\textsubscript{3}R models, we also assume a single IP\textsubscript{3} binding site in each subunit. The state of each subunit is denoted as (ijk), where the index i represents the IP\textsubscript{3}-binding site, j the activating Ca\textsuperscript{2+}-binding site, and k the inhibitory Ca\textsuperscript{2+}-binding site. An occupied state is represented as 1, and a nonoccupied site as 0.

The model further includes a conformational change whereby a subunit in the (110) state (one IP\textsubscript{3} and one activating Ca\textsuperscript{2+} bound) is “inactive”, and must transition to an “active” (A) state before it can contribute to channel opening. This conformational step is analogous to the well-characterized behavior of nicotinic acetylcholine receptors (21), and further implies that the active state is “locked” with respect to agonist binding and dissociation. Observations of ligand-independent flickerings of the IP\textsubscript{3}R channel to the closed state (11) are consistent with such a conformational change, and the lack of effect of changes in Ca\textsuperscript{2+} concentration on gating of already open IP\textsubscript{3}R channels (22) supports the notion that active subunits are locked with respect to ligand binding.

We also assume that the channel is open when either three or four subunits are in an active state. This assumption has previously been applied in some IP\textsubscript{3}R models (23), and we show here that it can explain the dependence of channel open time on ligand concentration. Although some multimeric channels show distinct conductance levels associated with ligand binding to differing numbers of subunits (24), the Xenopus oocyte IP\textsubscript{3}R displays only a single major conductance level (11,12), so we distinguish only a single open state, irrespective of whether three or four subunits are active.

Each subunit in the model has nine states, with transitions governed by second-order rate constants (a\textsubscript{i}, with i > 0) for binding processes, first-order rate constants (b\textsubscript{i}, with i > 0) for unbinding process, and constant transition rates (a\textsubscript{0} and b\textsubscript{0}) applied between the active A-state and the inactive (110) state (Fig. 1). Parameter values used in the model are listed in Table 1. Values for dissociation constants were chosen on the basis of optimal fit to steady-state experimental data from patch-clamped oocyte nuclear IP\textsubscript{3}R (Fig. 2). For all the binding/unbinding loops given in Fig. 1, the thermodynamic constraint of detailed balance requires that K\textsubscript{1}K\textsubscript{2} = K\textsubscript{3}K\textsubscript{4} for reaction dissociation constants. The conformation rate changes a\textsubscript{0} and b\textsubscript{0} between the (110) and active states of

![Image](https://example.com/image.png)
TABLE 1 Parameter values used in the IP3R channel model

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value (unit)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Conformation change rate</td>
<td>$a_0$ 540 s$^{-1}$, $b_0$ 80 s$^{-1}$</td>
</tr>
<tr>
<td>IP$_3$-binding site</td>
<td>$K_1$ 0.0036 μM, $a_1$ 60 μM$^{-1}$ s$^{-1}$, $K_3$ 0.8 μM, $a_3$ 5.0 μM$^{-1}$ s$^{-1}$</td>
</tr>
<tr>
<td>Activating calcium-binding site</td>
<td>$K_4$ 0.8 μM, $a_4$ 150 μM$^{-1}$ s$^{-1}$</td>
</tr>
<tr>
<td>Inhibitory calcium-binding site</td>
<td>$K_2$ 16 μM, $a_2$ 0.2 μM$^{-1}$ s$^{-1}$, $K_4$ 0.072 μM, $a_4$ 0.5 μM$^{-1}$ s$^{-1}$</td>
</tr>
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In the table, the disassociation constant $K_i = b_i/a_i$, with $a_i$ the on-binding rate and $b_i$ the off-binding rate. Due to the thermodynamic constraint, we have $K_1K_2 = K_3K_4$.

the subunits were chosen to give a maximum channel open probability of ~0.84, as observed experimentally for Xenopus oocyte nuclei (10,11). The rate constant for IP$_3$ binding was based on experimental measurements of first opening latencies of 0.35 and 0.5 s for IP$_3$R channels in Sf9 cell nuclei at [Ca$^{2+}$] = 2 μM after step increases in [IP$_3$] from 0 to 10 and 100 μM, respectively (K. Foskett and D. O. Mak; unpublished data). Model simulations of single channel latencies provided a good fit, with predicted corresponding mean latencies of 0.34 and 0.4 s. Rate constants for Ca$^{2+}$ binding were estimated by iterative fitting of model predic-

tions to published data of Xenopus oocyte IP$_3$R open- and closed-time distributions (10,11).

We explored the behavior of the IP$_3$R model using both deterministic, matrix transition analysis and stochastic simulation. The deterministic approach provides a rigorous analysis of statistical channel behavior, but cannot reveal the trajectory of openings and closings of an individual IP$_3$R. Because we wish to use the model as a building block to explore the contribution of stochastic single-channel behavior to cellular Ca$^{2+}$ signaling, we also performed stochastic simulations; an approach that has the further advantage of providing a more intuitive insight into channel behavior.

Deterministic analysis of the IP$_3$R model

The probability of subunits in state $ijk$ or (A) is denoted by $P_{ijk}$ or $P_A$, with $P_A + \sum P_{ijk} = 1$. By the mass action kinetics, the equations describing the subunit dynamics are written

$$\frac{dP}{dt} = PQ,$$

where $Q$ is the generator matrix (25) of transition rates and $P$ is the vector of probability of subunits. The open probability for an IP$_3$R is then given by

$$P_O = P_A + 4P_A^3(1 - P_A),$$

Mathematically, the equilibrium state is defined by $dP/dt = 0$. The equilibrium vector $\mathbf{w}$ satisfies $\mathbf{w}Q = 0$.

FIGURE 2 Stochastic and deterministic modeling of IP$_3$R dynamics, and comparison with steady-state experimental data. (A) Example of stochastic simulation of IP$_3$R channel gating (upper), and the corresponding numbers of subunits in the active state (lower) at [IP$_3$] = 10 μM and [Ca$^{2+}$] = 0.2 μM. Arrows mark openings that are associated with 4-related open states. (B) Graph shows the dependence of steady-state open probability ($P_O$) as a function of [Ca$^{2+}$] for different concentrations of IP$_3$. Solid curves show results by the deterministic transition matrix theory. The results obtained by stochastic simulation are represented by open symbols ([IP$_3$] = 10 μM (stars), 0.033 μM (circles), 0.02 μM (squares), and 0.01 μM (triangles)). Single-channel patch-clamp experimental data obtained from IP$_3$R on native nuclear membranes by Mak et al. (10,11) were replotted as solid symbols ([IP$_3$] = 10 μM (stars), 0.033 μM (circles); 0.02 μM (squares), and 0.01 μM (triangles)). (C and D) Mean open time $\tau_O$ (C) and closed time $\tau_C$ (D), respectively, as functions of [Ca$^{2+}$] for different concentrations of IP$_3$, as indicated. Solid curves show results obtained with transition matrix theory, and open symbols show stochastic simulation results. Solid stars show corresponding experimental data at [IP$_3$] = 10 μM (10,11).
Detailed balance is imposed so that we can solve for \( w \) by inspection (26). This is done by calculating all probabilities in terms of their probability relative to state (000). These unnormalized probabilities are denoted \( q_{ijk} \), with \( q_{0000} = 1 \). Then
\[
w_{ijk} = \frac{q_{ijk}}{Z}
\]
where each component \((q_{ijk}/Z)\) gives the equilibrium probability for state \((ijk)\). \( Z \) is the normalization factor defined by \( Z = q_A + \sum q_{ijk} \). The equilibrium probability \((q_{ijk})\) of state \((ijk)\) relative to that of state (000) is just the product of forward to backward rates along any path connecting (000) to \((ijk)\). Thus, we can write
\[
q_A = \frac{\left[ [\text{IP}_3] \times [\text{Ca}^{2+}] \right]}{K_1K_5} \times \frac{a_0}{b_0} \tag{4}
\]
and
\[
Z = \left(1 + \frac{[\text{Ca}^{2+}]}{K_4}\right) \left(1 + \frac{[\text{Ca}^{2+}]}{K_5}\right) + \frac{\left[ [\text{IP}_3] \times [\text{Ca}^{2+}] \right]}{K_1} \left(1 + \frac{[\text{Ca}^{2+}]}{K_4}\right) \left(1 + \frac{[\text{Ca}^{2+}]}{K_5}\right) + q_A. \tag{5}
\]

The equilibrium probability for the subunit active state is given by
\[
w_A = \frac{\left[ [\text{IP}_3] \times [\text{Ca}^{2+}] \right]}{K_1K_5} \times \frac{a_0}{b_0} \times \frac{1}{Z} \tag{6}
\]

Since the channel is open if either three or four subunits are active, the equilibrium open probability is a sum of contributions from three and four active subunits: \( p_3 = 4w_A^3 \) \((1 - w_A)\) and \( p_4 = w_A^4 \). Thus, the open probability at the equilibrium state for an IP₃R channel is
\[
P_O = w_A^4 + 4w_A^3(1 - w_A). \tag{7}
\]

Because channel states (A, A, A, not-A) are the only open states that connect to closed channel states by any one of three A-states changing to the closed state 110 with rate \( b_0 \), we can directly write the equilibrium probability flux between open and closed states as follows:
\[
J = 3b_0p_3. \tag{8}
\]

The mean open and closed times are given by
\[
\tau_O = \frac{P_O}{J} = \frac{1}{3b_0} \times \frac{P_O}{p_3} = \frac{1}{3b_0} \times \frac{1 + p_3}{p_3}
\]
\[
\tau_C = 1 - \frac{P_O}{J} = \frac{1}{3b_0} \times \frac{1 - P_O}{p_3}. \tag{9}
\]

Equation 9 implies that the channel mean open time varies even though the subunit mean active time is fixed. \( \tau_O \) has a limiting minimum value of \( 1/(3b_0) \) and increases as \( p_4/p_3 \) increases. This is to be expected since the channel is open if either three or four subunits are active but closes only when there are precisely three active subunits.

Deterministic solutions presented in Fig. 2 (showing the open probability \( P_O \), mean open time \( \tau_O \), and mean closed time \( \tau_C \) as functions of constant \( \text{Ca}^{2+} \) concentration at different \( \text{IP}_3 \)) were obtained using Eqs. 7 and 9. Furthermore, we applied the transition matrix theory to predict the open- and closed-time distributions of the channel in steady state and the distributions of the first-opening latency of individual and clustered IP₃Rs responding to step IP₃ stimulus. The analytic deductions employed to obtain those results will be described in detail in a separate article (J. Shuai, I. Parker, and J. E. Pearson; unpublished).

Stochastic simulation of the IP₃R model

We simulated the stochastic dynamics of this nine-state subunit channel model by a Markov process (27,28), updating the state of the system at small time steps \( dt \). For example, a channel subunit in the \((110)\) state at time \( t \) could transition to states \((010),(100),(111)\), or to the active A-state at the next time step \( t + dt \) with respective transition probabilities of \( b_0dt\), \( b_1dt\), \( a_2[\text{Ca}^{2+}] \times dt\), or \( a_0dt\); otherwise, it remains in the same state. Random numbers homogeneously distributed in \([0,1]\) were generated at each time step and compared with these transition probabilities to determine the state of the channel subunit at the next time step. The IP₃R channel is open when three or four subunits are in the A-state. A time step \( dt = 10 \mu s \) was generally used, being much shorter than mean channel open or closed times. The results were not appreciably different when \( dt \) was altered between 0.1 and 50 \( \mu s \), and the close correspondence obtained with results of the deterministic analysis further validates the simulation method.

RESULTS

Steady-state IP₃R dynamics

In this section, we describe the behavior of the single IP₃R model under steady-state conditions of given \([\text{IP}_3]\) and \([\text{Ca}^{2+}]\), and demonstrate that our model successfully reproduces the experimental data obtained from patch-clamped IP₃R on the Xenopus oocyte nuclear membrane (9–12).

An example of stochastic channel gating

Fig. 2 A illustrates stochastic channel gating, and the corresponding subunit states under conditions \([\text{IP}_3] = 10 \mu M\) and \([\text{Ca}^{2+}] = 0.2 \mu M\) that result in a mean open probability \((P_O)\) of ~0.4. Because the channel opens when either three or four subunits are active, we can distinguish two different types of channel open state: A₃-only openings and A₄-related openings. We define A₃-only openings as those involving only three simultaneously active subunits throughout the duration of the opening, whereas A₄-related
openings involve at least one occurrence of all four subunits being active (e.g., openings marked by arrows in Fig. 2 A).

**Dependence of open probability on [IP₃] and [Ca²⁺]**

The solid symbols in Fig. 2 B show experimental measurements from oocyte nuclei of the dependence of IP₃R channel open probability (P₀) as a function of cytosolic [Ca²⁺] for different concentrations of IP₃ (10,11). The data follow the well-known “bell-shape” distribution, with increasing concentrations of IP₃ producing a rightward shift in the Ca²⁺ concentration required for maximal P₀, and with the maximal P₀ increasing steeply for IP₃ concentrations between 10 and 33 nM. These experimental observations are fit reasonably well by our IP₃R model, as shown in Fig. 2 B by results obtained from both deterministic analysis (solid curves) and stochastic simulation (open symbols). An exception is that the model predicts a less steep dependence of P₀ at low values of [IP₃] than was experimentally observed.

A maximal P₀ = 0.84 was achieved with the model under optimal conditions ([IP₃] > 0.5 μM and [Ca²⁺] ≈ 3 μM). This corresponds well with measurements from IP₃R on the Xenopus oocyte nucleus (10,11), but is much greater than that (P₀ ≈ 0.2) observed for cerebellar IP₃R reconstituted in lipid bilayers (5). Concentrations of IP₃ >−0.5 μM are already saturating, as expected from the relatively high binding affinity (K_I = 0.0036 μM) in the model.

**Mean open and closed time**

The mean open (τ₀) and closed (τ_c) times of the IP₃R channel are plotted, respectively, in Fig. 2, C and D, as functions of Ca²⁺ and IP₃ concentrations for the deterministic (solid curves) and stochastic (open symbols) versions of the IP₃R model, together with experimental data (solid symbols) from oocyte nuclear receptors at [IP₃] = 10 μM (10). It is evident that the dependence of P₀ upon [Ca²⁺] and [IP₃] described in Fig. 2 B arises primarily through correspondingly large changes in τ_c, and the model results with 10 μM IP₃ fit well to the experimental observations. Additionally, although subject to appreciable scatter, the patch-clamp data also reveal a modest (two- to threefold) increase in τ₀ associated with increasing P₀ (10). This behavior is reproduced by our model (Fig. 2 C).

**Variation of mean open time on [IP₃] and [Ca²⁺]**

At first sight, the dependence of predicted τ₀ on ligand concentrations (Fig. 2 C) appears unexpected, given that the transition rate b₀ from the active A-state to the closed state (1110) of each subunit is a fixed value, resulting in a constant active dwell time of 1/b₀ for each subunit. Theory (Eq. 9) indicates that mean open time τ₀ varies with [Ca²⁺] and [IP₃] because the probability for being in the gateway states in which three subunits are active varies with respect to being in the single state with four active subunits. Indeed, the theory is in solid accord with the experimental data, in which the mean open time varies by about a factor of 2. The variation in τ₀ is given by the factor 1 + p₁/p₄ = 1 + wₐ/(4(1 − wₐ)) (see Eq. 9). The IP₃R is observed to have a maximum P₀ of ~0.84. To within a few percent, P₀ takes on its maximum value of 0.84 when wₐ is −0.8. This occurs when p₁ = p₄.

Thus, theory predicts that the channel mean open time varies by a factor of 2, in accord with observation. To further illustrate this point, we analyzed the results of stochastic simulations, and we show below that the variation in mean open time results because there are two populations of channel open states, involving only three simultaneously active subunits, or at least one occurrence of four active subunits.

We first determined the mean open times associated with each of these conformations. Fig. 3 A shows that mean open times for A3-only openings (Tₐ) and for A4-related openings (Tₐ) change only slightly as a function of [Ca²⁺] at [IP₃] = 10 μM, with respective values of ~2.6–4.2 and 14.5–15.5 ms. The mean open time Tₐ can be intuitively understood

![FIGURE 3 Dependence of τ₀ on ligand concentration can be explained by a change in the proportion of openings involving only three active subunits (A3-only openings) and those involving four active subunits (A4-related openings).](image)
because the channel will close when any one of the three active subunits becomes inactive, so that $T_{A3} \approx 1/(3b_0) \approx 4$ ms.

Because the mean dwell times of A3- only and A4-related openings have only a slight ligand dependence, the change in mean channel open time with ligand concentration must, therefore, involve also a change in proportion of A3- only and A4-related events. For example, with [$Ca^{2+}$] at an optimal value of $\sim 3 \, \mu M$, each subunit will have a high probability of being in the active state, thereby increasing the probability of finding four active subunits; whereas at lower [$Ca^{2+}$] the probability of subunits having Ca$^{2+}$ bound to the activating site is lower, and at higher [$Ca^{2+}$] there is an increasing chance of subunits becoming inhibited. Thus, the probability for A4-related openings, $P_{A4}$, first increases and then decreases with increasing [Ca$^{2+}$], and the probability for A3-only openings, $P_{A3}$, correspondingly follows an inverse relationship (Fig. 3 B).

The mean open time of the channel, expressed as

$$\tau_0 = P_{A3}T_{A3} + P_{A4}T_{A4},$$

therefore varies as a function of [Ca$^{2+}$] and [IP$_3$]. At very low and high [Ca$^{2+}$], the mean open time $\tau_0$ derives almost entirely from the A3-only open state, giving a value of $\tau_0 \approx 4$ ms. At the optimal value of [Ca$^{2+}$], $\sim 3 \, \mu M$, $P_{A3} \approx P_{A4} = 0.5$ (Fig. 3 B), so that $\tau_0 \approx 0.5 \times (T_{A3} + T_{A4}) \approx 9$ ms.

Open- and closed-time distributions

Patch-clamp experimental data show that open-channel dwell times follow a biexponential distribution, with time constants of $\sim 4$ ms and 20 ms (12). This behavior is predicted also by our model with stochastic simulation and deterministic theory, where the open-time distributions at various [Ca$^{2+}$] are approximated by a sum of two exponentials (Fig. 4 A). These two exponential components can be considered as arising from A3-only and A4-related openings. For example, the distributions of A3-only and A4-related open dwell times are plotted in Fig. 4 B for [Ca$^{2+}$] = 2 $\mu M$ and [IP$_3$] = 10 $\mu M$. The distribution of A3-only openings is monoeponential, with a time constant of $\sim 4$ ms, and the distribution of A4-related openings approximates an exponential with time constant of $\sim 12$ ms for openings $>10$ ms. For various [Ca$^{2+}$] at [IP$_3$] = 10 $\mu M$, time constants of A3-only and A4-related exponential open distribution are $\sim 3$–5 and 9–14 ms, respectively.

Patch-clamp experimental data show that the IP$_3$R channel has at least two closed states, with the time constants $\sim 1$ ms and 10 ms, as well as a long closed kinetic state with time constant of the order of seconds (12). Our model predicts also a rich kinetic behavior for closed dwell times. Three examples of closed-time distributions are plotted in Fig. 5 A for [Ca$^{2+}$] = 0.2, 2.0, and 200 $\mu M$ at [IP$_3$] = 10 $\mu M$. For [Ca$^{2+}$] = 0.2 $\mu M$ (Fig. 5 A, upper), three exponential components can be clearly distinguished at regions $t_c < 10$ ms, 20 < $t_c < 400$ ms, and $t_c > 450$ ms, with time constants of 1, 25, and 160 ms, respectively. For [Ca$^{2+}$] = 2.0 and 200 $\mu M$, the distributions can be approximated by two exponential functions: a fast component with time constant 1–3 ms and a slow component with time constants 200–300 ms. The faster component (time constant $\sim 2$ ms) derives largely from immediate, ligand-independent transitions from the (110) state of the model to the active state, as set by the time constant $1/\alpha_0$. The slower components derive from transitions involving the other seven closed states, and are expected to be correspondingly complex. In practice, we are able to discern only a maximum of three-exponential functions by fitting to predicted closed-time distributions.

The multiexponential distributions of closed times lead to a “burst-like” behavior of channel gating. During bursts of rapid openings, short closings arise largely as any one of three active subunits undergoes round-trip transitions through the (110) states, whereas the more prolonged interburst intervals result from subunits entering longer-lived inactive states that require ligand association or dissociation to return to the (110) state. A running average of instantaneous $P_O$ with a time
window of 100 ms thus shows large fluctuations over time (Fig. 5 B), similar to that observed experimentally (12).

**Puff latencies after steps of [IP\textsubscript{3}]**

In this article, we limit consideration of our IP\textsubscript{3}R model to conditions where [Ca\textsuperscript{2+}] is fixed at given values. The results are therefore not immediately applicable to cellular signaling, where cytosolic [Ca\textsuperscript{2+}] fluctuates widely owing to Ca\textsuperscript{2+} flux through the IP\textsubscript{3}Rs themselves. An exception, however, concerns experimental observations of Ca\textsuperscript{2+} puffs evoked by flash photorelease of IP\textsubscript{3}, where the mean puff latency shortens with increasing [IP\textsubscript{3}] (7,8). In this case, the basal cytosolic [Ca\textsuperscript{2+}] remains essentially unchanged before the puff, permitting us to simulate puff initiation by considering the stochastic variability in opening of an IP\textsubscript{3}R channel after a step increase in [IP\textsubscript{3}] at constant [Ca\textsuperscript{2+}]. We assume that opening of a single IP\textsubscript{3}R channel provides sufficient ‘‘trigger’’ Ca\textsuperscript{2+} to activate neighboring channels and thereby evoke a puff (29), and estimate the number of IP\textsubscript{3}R clustered at a puff site by fitting the stochastic simulation results to experimental data.

**Responses of a single IP\textsubscript{3}R channel to a step of [IP\textsubscript{3}]**

We first consider the latency of an individual channel after a step increase in IP\textsubscript{3} concentration. Initially, the channel is in equilibrium at biologically realistic resting conditions with cytosolic [Ca\textsuperscript{2+}]	extsubscript{Rest} = 0.1 \mu M and [IP\textsubscript{3}] = 0 \mu M. At time \( t = 0 \), the concentration of IP\textsubscript{3} increases instantaneously from 0 \mu M to [IP\textsubscript{3}]	extsubscript{Sim} to simulate the rapid photorelease of IP\textsubscript{3} by an ultraviolet flash. Examples of three responses to a step [IP\textsubscript{3}]	extsubscript{Sim} = 10 \mu M are presented in Fig. 6 A, illustrating the stochastic variability in channel kinetics. Here, we are concerned only with the latency to the first opening of the channel, and disregard subsequent openings. Fig. 6, B and C, plots distributions of channel first-opening latencies for various [IP\textsubscript{3}]	extsubscript{Sim} and [Ca\textsuperscript{2+}]	extsubscript{Rest} obtained from simulation and theory. The distributions follow skewed \( \Gamma \) -shaped curves that shift leftward and become narrower with increasing [IP\textsubscript{3}]	extsubscript{Sim} (Fig. 6 B) and [Ca\textsuperscript{2+}]	extsubscript{Rest} (Fig. 6 C).

The mean first-opening latency of the channel as a function of [IP\textsubscript{3}]	extsubscript{Sim} is shown in Fig. 7 A for [Ca\textsuperscript{2+}]	extsubscript{Rest} = 0.1 \mu M. The latency shortens markedly as [IP\textsubscript{3}]	extsubscript{Sim} increases from 0 to 5 \mu M, but then reaches a minimum value of \( \sim 400 \) ms at higher [IP\textsubscript{3}]	extsubscript{Sim}. The mean first-opening latency of the channel as a function of [Ca\textsuperscript{2+}]	extsubscript{Rest} is shown in Fig. 7 C for [IP\textsubscript{3}]	extsubscript{Sim} = 0.1 and 10 \mu M. An interesting observation is that changes in [Ca\textsuperscript{2+}]	extsubscript{Rest} from 0.05 to 0.2 \mu M cause an increase of the mean minimum latency at low [IP\textsubscript{3}]	extsubscript{Sim} (from \( \sim 2500 \) to \( \sim 3500 \) ms for [IP\textsubscript{3}]	extsubscript{Sim} = 0.1 \mu M), but a decrease of the latency at high [IP\textsubscript{3}]	extsubscript{Sim} (from \( \sim 650 \) to \( \sim 350 \) ms for [IP\textsubscript{3}]	extsubscript{Sim} = 10 \mu M).

These results can be understood in terms of the states of the IP\textsubscript{3}R subunit model. For very small [Ca\textsuperscript{2+}]	extsubscript{Rest} \( \leq 0.01 \) \mu M, >85\% channel subunits are in the (000) state at [IP\textsubscript{3}] = 0 \mu M. The binding of Ca\textsuperscript{2+} becomes rate-limiting, so that the latencies are long and have little dependence on [IP\textsubscript{3}]	extsubscript{Sim}. At physiological cytosolic [Ca\textsuperscript{2+}]	extsubscript{Rest} \( \sim 0.1 \) \mu M, an important result is that a large proportion of subunits are predicated to be in a Ca\textsuperscript{2+}-inhibited state (e.g., at [Ca\textsuperscript{2+}] = 0.2 \mu M and [IP\textsubscript{3}] = 0 \mu M, 75\% of subunits are in the (001) or (011) states) before flash photorelease of IP\textsubscript{3}. As a result, changes in basal [Ca\textsuperscript{2+}]	extsubscript{Rest} will have dual opposing effects on the latency, with increasing [Ca\textsuperscript{2+}]	extsubscript{Rest} both increasing the steady-state probability of subunits being in Ca\textsuperscript{2+}-inhibited states, and also speeding the binding of Ca\textsuperscript{2+} to the activating site. At physiological cytosolic [Ca\textsuperscript{2+}]	extsubscript{Rest}, our model shows that these two effects function differently at different [IP\textsubscript{3}]	extsubscript{Sim}. In particular, a fourfold change in [Ca\textsuperscript{2+}]	extsubscript{Rest} from 0.05 to 0.2 \mu M results in a small shortening of the mean latency for large [IP\textsubscript{3}]	extsubscript{Sim} and a small lengthening of the mean latency for small [IP\textsubscript{3}]	extsubscript{Sim} (Fig. 7 C).

**Responses of clustered IP\textsubscript{3}Rs to steps of [IP\textsubscript{3}]**

We next extend our simulation from a single IP\textsubscript{3}R channel to a cluster of \( N \) functionally independent channels representing
shorter for a given $[\text{IP}_3]_{\text{Stim}}$—as expected, since it represents the first among the 50 channels to open—but the general shape of the curve is similar.

An interesting observation is that the mean latency for clustered IP$_3$Rs for both large and small $[\text{IP}_3]_{\text{Stim}}$ at first shortens as $[\text{Ca}^{2+}]_{\text{Rest}}$ is raised from a low value (0.005 μM), but reaches a minimum at ~0.1 μM and thereafter actually shows a slight lengthening (Fig. 7 D). An explanation is that binding of Ca$^{2+}$ to activating sites is rate-limiting at very low $[\text{Ca}^{2+}]_{\text{Rest}}$ so that the latency first becomes shorter as $[\text{Ca}^{2+}]_{\text{Rest}}$ increases from 0.01 μM. However, at higher concentrations (>0.1 μM), there is an increasing likelihood of subunits being in an inhibited state due to $K_d = 0.072$ μM (Fig. 1), so that the latency approaches a minimal value set by the dissociation rate $b_2$ from inhibitory Ca$^{2+}$-binding sites.

Fig. 8 A shows the puff latency distributions obtained from theory and simulation for $[\text{IP}_3]_{\text{Stim}} = 10$ μM and $[\text{Ca}^{2+}]_{\text{Rest}} = 0.1$ μM considering clusters containing $N = 25, 50$, and 150 channels. The curves represent the stochastic variability in first-opening latencies, and since they reflect the population behavior of multiple channels, the peaks of the distributions shift to shorter latencies with increasing $N$ while the spread of the distribution narrows.

**Number of IP$_3$Rs at a puff site**

To compare model predictions with the experimental data, the mean puff latency $T_{\text{Puff}}$ is replotted as a function of $1/[\text{IP}_3]_{\text{Stim}}$ in Fig. 8 B for clusters of $N = 25, 50$, and 150 channels at $[\text{Ca}^{2+}]_{\text{Rest}} = 0.1$ μM, together with experimental data of puff latencies in *Xenopus* oocytes taken from Callamaras et al. (7) and Parker et al. (8). The experimental puff latency $T_{\text{Exp}}$ can be fit as a linear function of $1/[\text{IP}_3]_{\text{Stim}}$

\[ T_{\text{Exp}}(t_{\text{Sim}}) = T_0 + \frac{k}{t_{\text{Sim}}} \]  

with the minimal latency $T_0 = 41$ ms and slope $k = 16.5$ ms×μM (Fig. 8 B, solid line). Good agreement with these experimental data was obtained by simulating a cluster containing 50 IP$_3$R channels.

To better quantify the agreement between model and experimental measurements of puff latencies ($T_{\text{Model}}$ and $T_{\text{Exp}}$, respectively), we introduce an optimal matching function:

\[ \Theta(N, [\text{Ca}^{2+}]_{\text{Rest}}) = -\ln(\Phi(N, [\text{Ca}^{2+}]_{\text{Rest}})) \]

\[ \Phi = \frac{1}{M \sum_{[\text{IP}_3]_{\text{Sim}}^{-1}}^{[\text{IP}_3]_{\text{Sim}}} \left( \frac{T_{\text{Model}}(N, [\text{IP}_3]_{\text{Sim}}) - T_{\text{Exp}}([\text{IP}_3]_{\text{Sim}})}{T_{\text{Exp}}([\text{IP}_3]_{\text{Sim}})} \right)^2 } \]

A larger value of $\Theta$ indicates a better match between the modeled puff and the experimental observation.
The results are depicted graphically in Fig. 8C by contours of increasing Θ. Here we discuss the optimal function Θ by varying both the channel number N in the cluster and the resting Ca\(^{2+}\) concentration. The resting Ca\(^{2+}\) concentration in cytosol is \(\approx 0.05–0.2 \ \text{μM}\). An optimal region in the \(N-\left[\text{Ca}^{2+}\right]_{\text{Rest}}\) plane obtained with the model also centered at \(\left[\text{Ca}^{2+}\right]_{\text{Rest}} = 0.12 \ \text{μM}\) with \(N = 55\). Our simulation given in Fig. 8C suggests that the total channel number in a cluster may be in the range of 40 to 70 (considering the contour of \(\Theta = 2.0\) where \(\left[\text{Ca}^{2+}\right]_{\text{Rest}}\) is in the biologically realistic range of 0.05 to 0.2 μM).

**Effect of reduced triggering probability on puff latency**

In the above discussion, the puff latency was calculated assuming that the first opening of any single channel in a cluster invariably triggers a puff by CICR. However, it is likely that brief channel openings may provide insufficient ‘trigger’ calcium to initiate a puff. We thus explored the effect of reducing the probability of puff initiation by reducing the probability, \(P_{\text{Trigger}}\), that any given channel opening triggers a puff. Specifically, if the first opening of a channel within a cluster failed to trigger a puff, we then checked whether the next opening event (of the same or a different channel) triggered a puff with the same \(P_{\text{Trigger}}\), and so on, until a puff was evoked.

Our simulation shows that the average puff latency varies only slightly as a function of trigger probability, \(P_{\text{Trigger}}\), for \(P_{\text{Trigger}} \approx 30\%\). For example, the predicted cluster number \(N\) giving a good fit to the experimental data remained at \(\approx 50\) for \(P_{\text{Trigger}}>50\%\), increasing to \(N = 70\) for \(P_{\text{Trigger}} = 30\%\) and \(N = 100\) for \(P_{\text{Trigger}} = 20\%\).

**DISCUSSION**

We propose a dynamic model of the type-1 IP\(_3\) receptor in *Xenopus* oocytes, with the long-term goal of applying the model for stochastic simulations of cellular Ca\(^{2+}\) signaling dynamics within a realistic cytosolic environment. We specifically model the *Xenopus* oocyte system, as this is the subject of numerous cellular imaging studies (6–8,29) and a wealth of data are available from patch-clamp experiments on oocyte nuclear IP\(_3\)R (9–12).

Our model assumes that each IP\(_3\)R channel is comprised of four identical and independent subunits. Like the De Young-Keizer model (14), each subunit consists of two independent Ca\(^{2+}\)-binding sites—an activating and an inhibitory binding site—and one IP\(_3\) binding site. Furthermore, we assume that a subunit becomes ‘active’ after a conformational change that occurs after both IP\(_3\)-binding sites are occupied. The channel is open when at least three subunits are in the active state. The model provides a good fit to steady-state experimental data of channel-open probability \(P_{O} [\text{IP3}]\) (10,11), although it predicts a bell-shaped curve with \(\left[\text{Ca}^{2+}\right]\) even at high concentrations of IP\(_3\), different from the ‘flat-topped’ relationship obtained by Mak et al. (11) and Baran (20). Moreover, the model accounts well for the observed distributions of channel-open and -closed dwell times.

With the parameters given in Table 1, our model assumes that there is a negative allosteric interaction between the IP\(_3\) site and the inhibitory Ca\(^{2+}\) site, i.e., IP\(_3\) binding reduces the affinity of the inhibitory Ca\(^{2+}\) site (from \(K_{4,2}\) to \(K_{2,2}\)), and Ca\(^{2+}\) binding to the inhibitory site decreases the affinity of the IP\(_3\) site (from \(K_{1,1}\) to \(K_{1,2}\)). The affinity of the activating Ca\(^{2+}\) sites is independent of the inhibitory Ca\(^{2+}\)-binding and IP\(_3\)-binding sites.

In this article, we restrict consideration of the IP\(_3\)R model to situations where the Ca\(^{2+}\) concentration remains constant; the effects of feedback by Ca\(^{2+}\) flux through the channel will be considered in future publications. Nevertheless, the results provide novel insights into the functioning of both individual IP\(_3\)Rs and the population behavior of clusters of IP\(_3\)Rs at puff sites.
Channel opening by three out of four subunits

As is the case for numerous ion channels, the IP₃R is a multimer formed from several subunits. In some instances, exemplified by AMPA receptors (24), the single-channel conductance increases in a stepwise fashion as more subunits become active after binding of ligand. However, the Xenopus oocyte IP₃R displays only a single major conductance level (11,12), and our model correspondingly incorporates only a single open state. The question then arises as to how many of the four subunits must be active to open the channel.

We assume that the channel is open when either three or four subunits are in an “active” state. This assumption has previously been applied in some IP₃R models (23), and we also assume that there is only one conductance state, irrespective of whether three or four subunits are active. An alternative approach to our simple model has been used in allosteric modeling of the tetrameric IP₃ and ryanodine receptors (11,30). Such allosteric models are extremely complex because they consider different conductance states with different open probability corresponding to different number of subunits in the active state, which will involve numerous free parameters and be difficult to implement in stochastic simulations. The simulation shows that our simple IP₃R model can successfully reproduce two levels of experimental data obtained from patch-clamp of nuclear IP₃Rs and confocal imaging of clustered IP₃Rs.

One important consequence of assuming that channel openings occur with either three or four subunits in the active state is that this model successfully predicts the dependence of open dwell time on ligand concentrations, whereas if the channel opening requires all four active subunits to be in the active state, a ligand-independent, constant open dwell time would be expected, since the open time depends only on the backward rate constant b₀. The ligand dependence of mean open time can be intuitively understood by distinguishing two types of channel-open state, those involving only three active subunits (A₃-only), and those involving four active subunits (A₄-related). The mean dwell times in each state are relatively independent of ligand concentration, but A₄-related openings are much longer than A₃-only openings, since channel closure requires two subunits, rather than just one, to become inactive. Changes in mean channel open time thus derive from changes in the proportion of A₃-only and A₄-related openings.

FIGURE 8 Simulation and experimental measurements of puff latencies. (A) Predicted latency distribution of puffs for [IP₃]ₘₐₓ = 10 µM and [Ca²⁺]ₐₓₐₚₙ = 0.1 µM, assuming that a puff is evoked by the first opening of any IP₃R channel within clusters containing N IP₃Rs. The open symbols are for stochastic simulation results with N = 25 (inverted triangles), 50 (stars), or 150 (triangles). The corresponding solid curves are obtained from the transition matrix theory. (B) Predicted mean puff latencies as functions of [IP₃]ₘₐₓ are shown for clusters containing N = 25 (inverted triangles), 50 (stars), and 150 (triangles) channels, with [Ca²⁺]ₐₓₐₚₙ = 0.1 µM. For comparison, experimental data of puff latencies as a function of both the number of IP₃R in a cluster and the resting Ca²⁺ concentration. Optimal agreement (maximal value of the index Θ) is obtained with N = 40–70 and [Ca²⁺]ₐₓₐₚₙ = 0.05–0.2 µM.

The existence of distinct A₃-only and A₄-related openings may also explain experimental observations that the distributions of mean IP₃R channel open times follow two
exponential components (12). Mak et al. (12) proposed that these components arise from two kinetically distinguishable open states with different time constants, but our model suggests that they may instead reflect the different mean dwell times of A3-only and A4-related openings.

Furthermore, our model indicates a complex situation for the closed-time distribution. In principle, there are 486 distinct closed states and 9 distinct open states (J. Shuai, I. Parker, and J. E. Pearson; unpublished), but in practice, only two or three major exponential components can be discriminated from experimental or stochastic simulation data. The faster component primarily reflects brief closings caused by any one of the three active subunits undergoing multiple transitions between the active A-state and the inactive (110) state, whereas the slower components involve ligand binding transitions.

Inactivation of IP3R at basal cytosolic [Ca\(^{2+}\)]

One feature of the model is that the dissociation constant of the inhibitory Ca\(^{2+}\) binding site increases enormously from \(K_d = 0.072\) mM to \(K_d = 16\) mM after binding of IP3. This scheme is concordant with the conclusion of Mak et al. (10) that the effect of IP3 binding is not to directly activate the channel, as generally assumed, but rather to relieve the channel from Ca\(^{2+}\)-inhibition. A distinction, however, is that whereas Mak et al. (10) proposed that the sole action of IP3 is to reduce the effective affinity of the inhibitory Ca\(^{2+}\)-binding site, in our model it plays an additional role as an obligate agonist. That is to say, channel opening cannot occur in the absence of IP3 even if the inhibitory Ca\(^{2+}\) sites are unoccupied and the activating sites bind Ca\(^{2+}\) (11).

An important consequence of the high affinity of the inhibitory Ca\(^{2+}\) binding in the absence of IP3 is that a surprisingly high proportion of IP3Rs are predicted to be in a Ca\(^{2+}\)-inhibited state under basal resting cytosolic conditions with zero [IP3]. For example, with [Ca\(^{2+}\)]\(_{\text{Rest}}\) = 0.1 μM, ~60% of subunits would be Ca\(^{2+}\)-inhibited, resulting in ~82% of IP3Rs having two or more subunits in an inhibited state so that the channel cannot immediately open on binding of IP3 and activating Ca\(^{2+}\). Thus, the latency of Ca\(^{2+}\) responses evoked by a step increase of [IP3] will depend strongly on the dissociation of Ca\(^{2+}\) from inhibitory sites, as well the rates of association of Ca\(^{2+}\) and IP3 to activating sites. This is evident in Fig. 7 C, where the mean first-opening latency of a single IP3R initially shortens as [Ca\(^{2+}\)]\(_{\text{Rest}}\) is raised from a low value (0.005 μM), but reaches a minimum at ~0.05 μM and thereafter actually shows a slight lengthening in response to [IP3]\(_{\text{Sim}}\) = 0.1 μM. An explanation is that binding of Ca\(^{2+}\) to activating sites is rate-limiting at very low [Ca\(^{2+}\)]\(_{\text{Rest}}\) but that at biological concentrations of [Ca\(^{2+}\)]\(_{\text{Rest}}\) there is an increasing likelihood of subunits being in an inhibited state so that the latency approaches a minimal value set by the dissociation rate \(b_2\) from inhibitory Ca\(^{2+}\)-binding sites. Moreover, the magnitude of Ca\(^{2+}\) release will depend on the available fraction of noninactivated IP3Rs, which in turn will be a function of the resting [Ca\(^{2+}\)] before stimulation.

Number of IP3R at a puff site

Finally, we extrapolated our model from the individual IP3R to consider the latency of puffs generated by clusters containing multiple IP3Rs. On the assumptions that IP3Rs within a cluster are independent and that a puff is triggered by whichever channel in the cluster is the first to open, we obtained an optimal fit to experimental measurements of puff latency as a function of [IP3] (7,8) for clusters containing \(N = 40–70\) IP3Rs. This result is affected only slightly by changes of assumed resting Ca\(^{2+}\) concentration within a biologically realistic range of 0.05–0.2 μM.

The conclusion that clusters contain 40–70 IP3Rs likely represents a minimal estimate, since very brief channel openings may fail to initiate a puff, thereby requiring the number of IP3Rs in the model cluster to be increased to match the experimental data. However, this effect becomes appreciable only if the triggering probability is quite low. For example, our simulation shows that if channel openings have a 50% or better chance of initiating a puff \(P_{\text{Trigger}} > 50\%\), a cluster size with \(N \sim 50\) still gives a good fitting to the experimental data of puff latency. At smaller \(P_{\text{Trigger}}\), larger values of \(N\) are required to obtain a good fit to the experimental data; for example \(N = 70\) for \(P_{\text{Trigger}} = 30\%\). This treatment is simplified compared to the biological situation, where calcium lingering from a channel opening that failed to trigger a puff would likely increase the probability of a subsequent opening to trigger a puff. However, in our simulation, for simplicity, we assume that all the opening events for all the channels in the cluster has the same probability \(P_{\text{Trigger}}\) to trigger a puff; and that the resting calcium concentration is always fixed no matter how many opening channels failed to trigger a puff. We plan to address this question more fully in a future study by considering the stochastic dynamics of clustered channels, incorporating the feedback of released Ca\(^{2+}\) ions.

It should be noted that these values estimate the total number of IP3Rs clustered at a puff site. In contrast, most experimental work has used measurements of puff amplitudes to estimate the number of open IP3R channels that contribute to the Ca\(^{2+}\) flux during a puff. For example, we recently capitalized on the discovery of “trigger” events that may represent the opening of a single IP3R channel that initiates a puff (31) to construct a deterministic puff model that predicts the involvement of some 25–35 open channels (29). Thus, it is likely that only a minority of IP3Rs in a cluster open during a puff, as is expected if many receptors are inactivated at resting cytosolic [Ca\(^{2+}\)] and Ca\(^{2+}\) dissociates from inhibitory binding sites only slowly on the timescale of puff latencies (a few hundred milliseconds or shorter).

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